
(a) Two states of a switch

(b) Symbol for a switch

Figure 2.1 A binary switch

(a) Simple connection to a battery

(b) Using a ground connection as the return path

Figure 2.2 A light controlled by a switch

(a) The logical AND function (series connection)

(b) The logical OR function (parallel connection)

Figure 2.3 Two basic functions


Figure 2.4 A series-parallel connection


Figure 2.5 An inverting circuit

| $x_{1}$ | $x_{2}$ | $x_{1} \cdot x_{2}$ | $x_{1}+x_{2}$ |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 |
| 1 | 1 | 1 | 1 |
| AND |  |  |  |
| OR |  |  |  |

Figure 2.6 A truth table for AND and OR

| $x_{1}$ | $x_{2}$ | $x_{3}$ | $x_{1} \cdot x_{2} \cdot x_{3}$ | $x_{1}+x_{2}+x_{3}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 | 1 |
| 0 | 1 | 0 | 0 | 1 |
| 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 |

Figure 2.7 Three-input AND and OR


(a) AND gates

(b) OR gates

(c) NOT gate

Figure 2.8 The basic gates


Figure 2.9 An OR-AND function

(a) Network that implements $\quad f=\bar{x}_{1}+x_{1} \cdot x_{2}$

| $x_{1}$ | $x_{2}$ | $f\left(x_{1}, x_{2}\right)$ |
| :---: | :---: | :---: |
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

(b) Truth table for $f$

Figure 2.10 a Logic network


Figure 2.10 b Logic network

| $x$ | $y$ | $x \cdot y$ | $\overline{x \cdot y}$ | $\bar{x}$ | $\bar{y}$ | $\bar{x}+\bar{y}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 1 | 1 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 0 | $\underbrace{}_{\text {LHS }}$ | $\underbrace{}_{\text {RHS }}$ | 0 |
| 0 |  |  |  |  |  |  |

Figure 2.11 Proof of DeMorgan's theorem

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Figure 2.12 The Venn diagram representation

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Figure 2.13 Verification of the distributive property

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Figure 2.14 Verification example

| $x_{1}$ | $x_{2}$ | $f\left(x_{1}, x_{2}\right)$ |
| :---: | :---: | :---: |
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

Figure 2.15 A function to be synthesized

(a) Canonical sum-of-products

(b) Minimal-cost realization

Figure 2.16 Two implementations of a function

| Row <br> number | $x_{1}$ | $x_{2}$ | $x_{3}$ | Minterm | Maxterm |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | $m_{0}=\bar{x}_{1} \bar{x}_{2} \bar{x}_{3}$ | $M_{0}=x_{1}+x_{2}+x_{3}$ |
| 1 | 0 | 0 | 1 | $m_{1}=\bar{x}_{1} \bar{x}_{2} x_{3}$ | $M_{1}=x_{1}+x_{2}+\bar{x}_{3}$ |
| 2 | 0 | 1 | 0 | $m_{2}=\bar{x}_{1} x_{2} \bar{x}_{3}$ | $M_{2}=x_{1}+\bar{x}_{2}+x_{3}$ |
| 3 | 0 | 1 | 1 | $m_{3}=\bar{x}_{1} x_{2} x_{3}$ | $M_{3}=x_{1}+\bar{x}_{2}+\bar{x}_{3}$ |
| 4 | 1 | 0 | 0 | $m_{4}=x_{1} \bar{x}_{2} \bar{x}_{3}$ | $M_{4}=\bar{x}_{1}+x_{2}+x_{3}$ |
| 5 | 1 | 0 | 1 | $m_{5}=x_{1} \bar{x}_{2} x_{3}$ | $M_{5}=\bar{x}_{1}+x_{2}+\bar{x}_{3}$ |
| 6 | 1 | 1 | 0 | $m_{6}=x_{1} x_{2} \bar{x}_{3}$ | $M_{6}=\bar{x}_{1}+\bar{x}_{2}+x_{3}$ |
| 7 | 1 | 1 | 1 | $m_{7}=x_{1} x_{2} x_{3}$ | $M_{7}=\bar{x}_{1}+\bar{x}_{2}+\bar{x}_{3}$ |

Figure 2.17 Three-variable Minterms and Maxterms

| Row <br> number | $x_{1}$ | $x_{2}$ | $x_{3}$ | $f\left(x_{1}, x_{2}, x_{3}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 |
| 1 | 0 | 0 | 1 | 1 |
| 2 | 0 | 1 | 0 | 0 |
| 3 | 0 | 1 | 1 | 0 |
| 4 | 1 | 0 | 0 | 1 |
| 5 | 1 | 0 | 1 | 1 |
| 6 | 1 | 1 | 0 | 1 |
| 7 | 1 | 1 | 1 | 0 |

Figure 2.18 A three-variable function

(a) A minimal sum-of-products realization

(b) A minimal product-of-sums realization

Figure 2.19 Two realizations of a function

| $x_{1}$ | $x_{2}$ | $x_{3}$ | $f$ |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 0 |
| 1 | 1 | 1 | 1 |

Figure 2.20 Truth table for a three-way light controller


Figure 2.21 SOP implementation of the three-way light controller

(b) Product-of-sums realization

Figure 2.21 POS implementation of the three-way light controller

| $s$ | $x_{1}$ | $x_{2}$ | $f\left(s, x_{1}, x_{2}\right)$ |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 |
| 1 | 1 | 1 | 1 |

(a)Truth table

(c) Graphical symbol

(b) Circuit

(d) More compact truth-table representation

Figure 2.22 Multiplexer


Figure 2.23 Screen capture of the Waveform Editor


Figure 2.24 Screen capture of the Graphic Editor

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Figure 2.25 The first stages of a CAD system


ENTITY example1 IS
PORT ( $\mathrm{x} 1, \mathrm{x} 2, \mathrm{x} 3$ : IN BIT ; f : OUT BIT ) ;
END example1;
ARCHITECTURE LogicFunc OF example1 IS BEGIN
$\mathrm{f}<=(\mathrm{x} 1$ AND x2) OR (NOT x2 AND x3) ; END LogicFunc ;

Figure 2.26 A simple logic function and corresponding VHDL code

```
ENTITY example2 IS
    PORT ( x1, x2, x3, x4 : IN BIT ;
    f,g :OUT BIT );
END example2 ;
```

ARCHITECTURE LogicFunc OF example2 IS
BEGIN
$\mathrm{f}<=$ ( x 1 AND x 3 ) OR (NOT x3 AND x 2 ) ;
$\mathrm{g}<=($ NOT x3 OR x1) AND (NOT x3 OR x4) ;
END LogicFunc ;

Figure 2.30 VHDL code for a four-input function


Figure 2.31 Logic circuit for four-input function

(a)

(b)

Figure P2. 1 Two attempts to draw a four-variable Venn diagram


Figure P2.2 A four-variable Venn diagram


Figure P2.3 A timing diagram representing a logic function


Figure P2.4 A timing diagram representing a logic function

